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Changing impact of shocks: a time-varying proxy SVAR approach

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Abstract

In this paper we extend the Bayesian Proxy VAR to incorporate time variation in the parameters. A Gibbs sampling algorithm is provided to approximate the posterior distributions of the model's parameters. Using the proposed algorithm, we estimate the time-varying effects of taxation shocks in the US and show that there is limited evidence for a structural change in the tax multiplier.

Key words: Time-Varying parameters, Stochastic volatility, Proxy VAR, tax shocks

JEL codes: C2,C11, E3

1 Introduction

Temporal changes in macroeconomic dynamics and evolution in the propagation of economic shocks have been documented in numerous recent studies. In their seminal paper, Cogley and Sargent (2005) introduce a vector autoregression (VAR) with time-varying parameters and stochastic volatility (TVP-VAR) and provide evidence supporting shifts in the persistence and volatility of key US macroeconomic variables. Their model was extended by Primiceri (2005) who also allowed the

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contemporaneous coefficients of the VAR model to change over time thus allowing these models to be used for structural analysis. For example, using this model Benati and Mumtaz (2007) identify demand and supply shocks via sign restrictions to investigate the causes of the ‘Great Moderation’ in the US. Similarly, Baumeister and Peersman (2013) identify oil supply and demand shocks using sign restrictions and show that the price elasticity of oil demand in the US has declined over time. Gali and Gambetti (2009) employ TVP-VARs with long-run restrictions to investigate changes in US macroeconomic dynamics. Canova and Forero (2015) provide a general algorithm to estimate TVP-VARs when the shocks are identified via non-recursive identification schemes.

In parallel to this literature on TVP-VARs, the methods used for shock identification in VAR models have also seen rapid development. An approach that has gained popularity in recent empirical applications is the identification of shocks by using external instruments. This ‘proxy SVAR’ model was introduced by Mertens and Ravn (2013) and Stock and Watson (2008) and differs from standard identification methods because the contemporaneous impulse response is estimated using an instrumental variable procedure where the instrument is an exogenous proxy for the shock of interest, usually constructed via a narrative approach. This reliance on external information reduces the number of (possibly controversial) restrictions needed to identify the contemporaneous impulse response. As the proxy is used as an instrument and not an endogenous variable directly in the VAR, the effects of measurement error in the proxy can be alleviated. This feature of the model to combine SVARs with a more narrative approach to estimating causal effects is the key reason behind the increased popularity of proxy SVAR models in applied work.

In this paper, we propose an algorithm for the estimation of proxy SVAR models when the parameters of the model are allowed to vary over time, therefore extending the range of methods for time-varying SVARs described in Canova and Forero (2015). We provide a Gibbs sampling algorithm to approximate the posterior distributions of the parameters. Our estimation procedure

extends the Bayesian MCMC algorithm of Caldara and Herbst (2016) for fixed coefficient proxy SVAR models, by casting it in state space, and applying a ‘state of the art’ particle Gibbs algorithm to filter through the parameter time variation in the resulting nonlinear state space. We design a small simulation exercise to study the finite sample properties of our proposed algorithm showing that it displays a satisfactory performance.

Using the proposed model, we investigate the effects of tax shocks on the US economy and whether these effects have changed over time. To identify the tax shocks we use the narrative measure proposed by Mertens and Ravn (2012) as an instrument. Our results suggest that the response of GDP to a tax shock has declined over time but this mainly reflects a decline in the volatility of the shock rather than a structural change in the fundamental transmission mechanism of the shock.

The remainder of the paper is organised as follows. Section 2 presents the proxy SVAR model with time-varying parameters. Section 3 describes the particle Gibbs algorithm and provides a small Monte Carlo exercise to evaluate the performance of the proposed algorithm. Finally, Section 4 contains our empirical analysis on tax shocks in the US, and Section 5 includes some concluding remarks.

2 The time-varying proxy SVAR

We consider the following Gaussian VAR model with time-varying parameters:

$$Y_t = B_t X_t + u_t, \quad u_t = \Sigma_t^{1/2} \varepsilon_t, \quad \varepsilon_t \sim \mathcal{N}(0, I_N) \quad (1)$$

where Y_t is a $N \times 1$ matrix of endogenous variables, $X_t = [Y'_{t-1}, \dots, Y'_{t-P}, 1]'$ is $(NP + 1) \times 1$ matrix of regressors in each equation and B_t denotes the $N \times (NP + 1)$ matrix of coefficients

$B_t = [B_{1t}, \dots, B_{Pt}, c_t]$. This VAR model features time-varying autoregressive coefficients B_t , where we follow the literature in assuming that the evolution of the $N(NP + 1) \times 1$ vector $b_t := \text{vec}(B_t')$ is described through a random walk transition equation:

$$b_t = b_{t-1} + Q_b^{1/2} \eta_t^b, \quad \eta_t^b \sim \mathcal{N}(0, I_{N(NP+1)}), \quad (2)$$

where Q_b is assumed to be diagonal. The time-varying covariance matrix of the reduced form residuals u_t can be written as:

$$\Sigma_t = (A_t q)(A_t q)' \quad (3)$$

where A_t is a lower triangular matrix with time-varying elements, and q is an element of the family of orthogonal matrices of size N , satisfying $q'q = I_N$. By considering all possible values of q , the matrix $A_t q$ spans the space of all possible contemporaneous matrices; a result which follows from the QR decomposition of a square matrix.

Next, we decompose A_t as:

$$A_t = \tilde{A}_t H_t^{1/2} \quad (4)$$

where \tilde{A}_t is a lower triangular matrix with diagonal elements equal to one and H_t is diagonal. Following Primiceri (2005), we model the evolution of the unrestricted elements of \tilde{A}_t (where we denote by the vector a_t the $N(N-1)/2 \times 1$ elements below the subdiagonal of \tilde{A}_t) as random walks:

$$\alpha_t = \alpha_{t-1} + Q_a^{1/2} \eta_t^a, \quad \eta_t^a \sim \mathcal{N}(0, I_{N(N-1)/2}). \quad (5)$$

Finally, we assume that the diagonal elements of H_t (summarised in an $N \times 1$ vector h_t) evolve as

geometric random walks:

$$\ln h_t = \ln h_{t-1} + Q_h^{1/2} \eta_t^h, \quad \eta_t^h \sim \mathcal{N}(0, I_N). \quad (6)$$

2.1 Identification of shocks

The structural shocks of the VAR model ε_t are defined as

$$\varepsilon_t = A_{0,t}^{-1} u_t, \quad (7)$$

where $A_{0,t} = A_t q$. We assume, without loss of generality, that we are interested in identifying the first shock ε_{1t} in the $N \times 1$ vector of shocks $\varepsilon_t = [\varepsilon_{1t}, \varepsilon_{.t}]$, where $\varepsilon_{.t}$ contains the remaining $N - 1$ elements in ε_t . To do this, we employ an instrument m_t described by the following equation:

$$m_t = \beta \varepsilon_{1t} + \sigma v_t, \quad v_t \sim \mathcal{N}(0, 1) \quad (8)$$

where $\mathbb{E}(v_t \varepsilon_t) = 0$. The instrument is assumed to be relevant ($\beta \neq 0$) and uncorrelated with other structural shocks ($\mathbb{E}(m_t \varepsilon_{.t}) = 0$). As discussed in Caldara and Herbst (2016), the relevance of the instrument can be judged by calculating the reliability statistic of Mertens and Ravn (2013) which is defined as the squared correlation between m_t and ε_{1t} :

$$\rho = \frac{\beta^2}{\beta^2 + \sigma^2} \quad (9)$$

While we write equation 8 as a fixed coefficient model in the benchmark case, our procedure easily allows the extension to a time-varying β and σ^2 . For example one can assume that:

$$\beta_t = \beta_{t-1} + \sigma^\beta n_t^\beta, \quad n_t^\beta \sim \mathcal{N}(0, 1) \quad (10)$$

$$\ln \sigma_t^2 = \ln \sigma_{t-1}^2 + \sigma^\sigma n_t^\sigma, \quad n_t^\sigma \sim \mathcal{N}(0, 1) \quad (11)$$

This extended formulation would also allow the reliability statistic to change over time.

2.1.1 The likelihood function and the role of the instrument

The covariance between the reduced form residuals and the instrument can be defined by:

$$\begin{pmatrix} u_t \\ m_t \end{pmatrix} | L_t \sim \mathcal{N}(0, L_t L_t'), \quad L_t = \begin{pmatrix} A_t q & 0 \\ \bar{b} & \sigma \end{pmatrix} \quad (12)$$

where \bar{b} is a $1 \times N$ vector $\bar{b} = \begin{bmatrix} \beta & 0 & \dots & 0 \end{bmatrix}$, since

$$\begin{pmatrix} u_t \\ m_t \end{pmatrix} = L_t \begin{pmatrix} \varepsilon_t \\ v_t \end{pmatrix}.$$

To consider the role of the instrument we follow Caldara and Herbst (2016) and factor the likelihood of the model as:

$$p(Y_t, m_t | \Xi) = p(Y_t | \Xi) p(m_t | Y_t, \Xi) \quad (13)$$

where Ξ denotes all parameters and states of the model. Given the conditional normality assumption in equation 12, the conditional density $p(m_t | Y_t, \Xi)$ is also normal with mean $\mu_t = \beta q_1' A_t^{-1} u_t$ and variance $s = \sigma^2$, where q_1 is the first column of q .

As discussed in Caldara and Herbst (2016), μ_t can be interpreted as a linear combination of the orthogonalised residuals $A_t^{-1}u_t$. In the context of estimation, this means that draws from the posterior distribution that result in the difference between the proxy and this linear combination becoming smaller are given larger weight.

The key contribution of the current paper relative to Caldara and Herbst (2016) is that we embed the dependence on m_t within a state-space model. In our model, time-variation in the reduced-form of the model is enabled through A_t and B_t . However, the draws of q_1 ensure that the contemporaneous impact matrix $A_{0,t}$ accounts for the conditional likelihood of m_t .

The proposed model is related to recent contribution by Paul (2017) who incorporates proxies as exogenous variables in a time-varying VAR. He shows that this VARX approach leads to a consistent estimator of the relative or normalised impulse response. While the approach in Paul (2017) is attractive due to its simplicity, our model offers two advantages. First, since we use the proxy as an instrument, we can estimate reliability statistics and provide evidence on instrument relevance. Second, as we describe below, our procedure can easily accommodate missing values in the instrument series, and thus deal with an issue that is common in the existing literature.

It is also interesting to note that the literature on fixed coefficient Bayesian proxy SVARs has also considered alternative specifications for the model. In particular, Drautzburg (2016) and Rogers *et al.* (2016) link the instrument to the reduced form residuals and use $cov(u_t, m_t)$ to back out the implied normalised impulse vector. However, in a time-varying model, this formulation can be problematic as it is difficult to separate changes in the transmission mechanism and possible shifts in instrument reliability. Therefore, we use the specification proposed in Caldara and Herbst (2016) as our starting point.

3 Estimation

The model is estimated using a Metropolis-within-Gibbs algorithm. In this section we describe the priors and provide a sketch of the algorithm with details of the conditional posteriors given in the technical Appendix.

3.1 Priors and starting values

Following Cogley and Sargent (2005) and Primiceri (2005), we set the prior for Q_b using a training of sample of T_0 observations. Denote the OLS estimates of the VAR coefficients and coefficient covariance as B_{OLS} and V_{OLS} . The prior for Q_b is inverse-Wishart $\mathcal{IW}(T_0 \times V_{OLS} \times \kappa_b, T_0)$ where the scaling parameter is $\kappa_b = 3.5 \times 10^{-4}$. We set the initial value $b_{0|0} \sim \mathcal{N}(B_{OLS}, V_{OLS})$. The prior for Q_a is inverse Wishart: $\mathcal{IW}(I_{N(N-1)/2} \times \kappa_a, T_{a,0})$ where $\kappa_a = 1 \times 10^{-4}$. The prior for Q_h is also inverse Wishart: $\mathcal{IW}(I_N \times \kappa_h, T_{h,0})$ where $\kappa_h = 1 \times 10^{-4}$. To obtain an initial draw for these state variables we run the algorithm for a standard TVP-VAR for a limited number of iterations and use the last draw as the initial value to be input into the MCMC algorithm described below.

Following Caldara and Herbst (2016), the prior for q is uniform and as described in Rubio-Ramirez *et al.* (2010) can be sampled from by taking the QR decomposition of a $N \times N$ matrix from the standard normal distribution. When fixed parameters for equation 8 are used, we employ a standard Normal-inverse Gamma prior: $p(\beta) \sim \mathcal{N}(\beta_0, V_\beta)$ and $p(\sigma^2) \sim \mathcal{IG}^*(\sigma_0, v_0)$ where \mathcal{IG}^* is an inverse gamma density, re-parameterised in terms of the mean σ_0 and variance v_0 .

3.2 Gibbs sampling algorithm

The Gibbs sampling algorithm cycles through the following conditional posterior distributions:

Step 1. $p(A_t | \Xi_{-A_t}, Y_{1:T}, m_{1:T})$. Note that Ξ_{-A_t} denotes the set of all parameters other than A_t .

Conditional on Ξ_{-A_t} , the state-space model can be written as:

$$\begin{aligned}
Y_t &= B_t X_t + u_t \text{ observation} \\
u_t &= A_t q \varepsilon_t \text{ observation} \\
m_t &= \beta \varepsilon_{1t} + \sigma v_t \text{ observation} \\
\alpha_t &= \alpha_{t-1} + Q_a^{1/2} n_t^a \text{ transition} \\
\ln h_t &= \ln h_{t-1} + Q_h^{1/2} n_t^h \text{ transition}
\end{aligned} \tag{14}$$

The state-space in (14) is non standard due to non-linearity of the first observation equation and because of the relationship between the instrument and ε_{1t} . Therefore, to sample $[\alpha'_t, \ln h'_t]'$ we employ a particle-Gibbs sampler. In a seminal contribution, Andrieu *et al.* (2010) show how a version of the particle filter, conditioned on a fixed trajectory for one of the particles can be used to produce draws that result in a Markov kernel with a target distribution that is invariant. We employ a version of the sampler introduced in Lindsten *et al.* (2014) who propose the addition of a step that involves sampling the ‘ancestors’ or indices associated with the particle that is been conditioned on. They show that this leads to a considerable improvement in the mixing of the algorithm even with a few particles.

Step 2. $p(b_t | \Xi_{-b_t}, Y_{1:T}, m_{1:T})$. Given Ξ_{-b_t} containing all parameters except b_t , the state-space of the model can be written as:

$$\begin{aligned}
\begin{pmatrix} Y_t \\ m_t \end{pmatrix} &= \begin{pmatrix} I_N \otimes X_t' \\ 0 \end{pmatrix} b_t + \begin{pmatrix} u_t \\ m_t \end{pmatrix} \text{ observation} \\
b_t &= b_{t-1} + Q_b \eta_t^b \text{ transition}
\end{aligned}$$

where the conditional covariance matrix of the observation equation residuals is:

$$\text{cov} \left(\begin{array}{c} u_t \\ m_t \end{array} \middle| \Xi_{-b_t} \right) = \begin{pmatrix} A_t A_t' & A_t q_1' \beta \\ \beta q_1 A_t' & \beta^2 + \sigma^2 \end{pmatrix}$$

This system is conditionally linear and Gaussian and we can use the Carter and Kohn (1994) algorithm to draw b_t from its posterior distribution.

Step 3. $p(q_1 | \Xi_{-q_1}, Y_{1:T}, m_{1:T})$. Following Caldara and Herbst (2016), we use an independence Metropolis step to sample q_1 .

Step 4. $p(\beta, \sigma | \Xi_{-[\beta, \sigma]}, Y_{1:T}, m_{1:T})$. The structural shock of interest ε_{1t} can be calculated as $\varepsilon_{1t} = A_t q_1 u_t'$. First draw $p(\sigma^2 | \Xi_{-[\beta, \sigma]}, Y_{1:T}, m_{1:T})$. Assuming an inverse-Gamma prior, this conditional posterior is also inverse-Gamma and can be easily sampled from. If σ^2 is allowed to vary over time, the a Metropolis algorithm or a particle Gibbs step can be employed to sample from the conditional posterior. Moreover, conditioning on σ^2 equation 8 is a standard linear regression and conditional posterior which is Gaussian: $p(\beta | \Xi_{-[\beta, \sigma]}, \sigma, Y_{1:T}, m_{1:T}) \sim \mathcal{N}(M, V)$. Note that if β were allowed to be time-varying, the Carter and Kohn (1994) algorithm can be used to draw from its conditional posterior.

Step 5. Draw from $p(Q_b | \Xi_{-Q_b}, Y_{1:T}, m_{1:T})$, $p(Q_a | \Xi_{-Q_a}, Y_{1:T}, m_{1:T})$ and $p(Q_h | \Xi_{-Q_h}, Y_{1:T}, m_{1:T})$. Assuming an inverse-Wishart posterior, these conditional distribution are also inverse-Wishart and these draws are standard.

Step 7. $p(m_{-t} | \Xi_{m_{-t}}, Y_{1:T}, m_{1:T})$. This step is implemented if the instrument contains missing observations (denoted by m_{-t}). As in step 2, the model can then be written in the form of a conditionally linear, Gaussian state-space model with m_{-t} treated as a latent state. The Carter and Kohn (1994) algorithm can be used to draw the conditional posterior distribution.

3.3 Estimation using simulated data

To test the algorithm we conduct a simple simulation experiment. We generate data from the following data generating process:

$$Y_t = B_t Y_{t-1} + (A_t q) \varepsilon_t, \quad \varepsilon_t \sim \mathcal{N}(0, I_3) \quad (15)$$

where Y_t is 3×1 , $q'q = I_3$ and $A_t = \tilde{A}_t H_t^{1/2}$. The time-varying parameters evolve as:

$$\begin{aligned} \text{vec}(B'_t) &= \text{vec}(B'_{t-1}) + Q_b^{1/2} \eta_t^b, \quad Q_b = I_{N^2} \times 0.0001, \quad \eta_t^b \sim \mathcal{N}(0, I_{N^2}) \\ \alpha_t &= \alpha_{t-1} + Q_a^{1/2} \eta_t^a, \quad Q_a = I_{N(N-1)/2} \times 0.01, \quad \eta_t^a \sim \mathcal{N}(0, I_{N(N-1)/2}) \\ \ln h_t &= \ln h_{t-1} + Q_h^{1/2} \eta_t^h, \quad Q_h = I_N \times 0.01, \quad \eta_t^h \sim \mathcal{N}(0, I_N) \end{aligned}$$

where α_t denote the non-zero and non-one elements of the lower triangular matrix \tilde{A}_t and h_t are the diagonal elements of the diagonal matrix H_t . The instrument is generated via:

$$m_t = 0.2\varepsilon_{1t} + 0.1^{1/2}v_t, \quad v_t \sim \mathcal{N}(0, 1)$$

where ε_{1t} is the first element of ε_{1t} , the shock of interest. We generate 320 observations, from which we discard the first 100. We use 20 as a training sample, leaving 200 observations for estimation. The estimation of the model uses 5000 Gibbs iterations with a burn-in of 3000 iterations. The particle Gibbs step uses 10 particles. We repeat the simulation experiment 500 times with the state-variables kept constant in each iteration.

Figure 1 presents the true impulse response of all three variables to the structural shock ε_{1t} at horizon 0 and 20 and the estimated values. Although the estimated time-varying response is smoother than the true response, the estimates tracks the main structural shifts fairly well

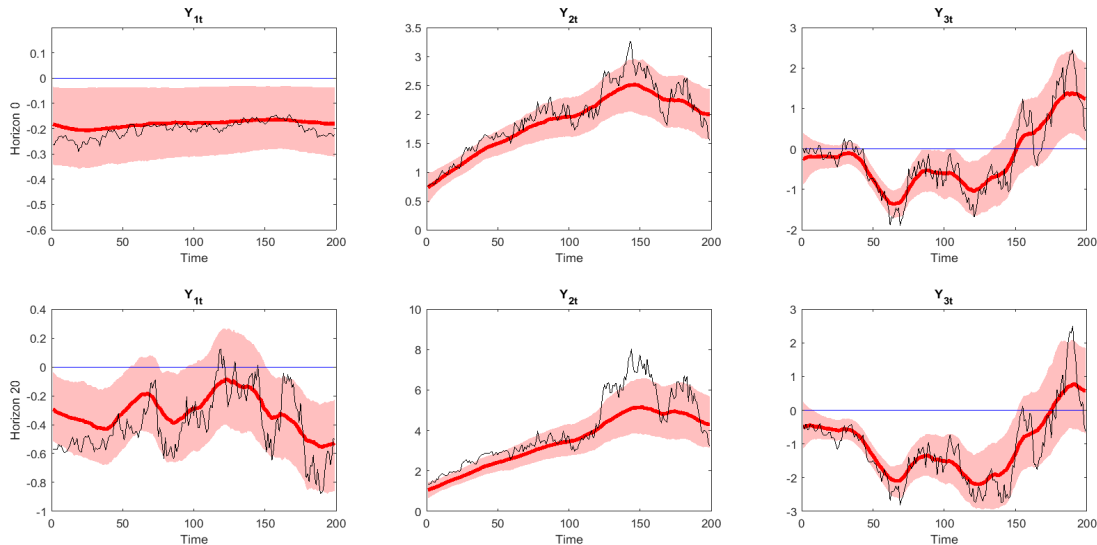


Figure 1: Impulse response to a 1 standard deviation shock to the first equation. The thick (red) line and shaded area represents the median and 1 standard deviation error band while the thin (black) line shows the true response.

providing some evidence that the MCMC algorithm proposed in this paper displays a satisfactory performance.

4 The time-varying impact of taxation shocks in the United States

The impact of tax shocks on output has received considerable attention in the recent macroeconomic literature. As pointed out in Mertens and Ravn (2014), estimates of the tax multiplier differ substantially with studies using narrative measures of tax shocks reporting estimates that are larger than those obtained using SVARs with zero restrictions. Mertens and Ravn (2014) propose a proxy SVAR to estimate the impact of taxation shocks. Their instrument is a refined version of the narrative tax measure of Romer and Romer (2010), the construction of which is described in Mertens and Ravn (2012). Romer and Romer (2010) build their shock measure by purging legislated tax changes from movements that are endogenous and driven by policy makers' concerns about growth. However, Mertens and Ravn (2012) argue that the Romer and Romer (2010) tax shock may not satisfy exogeneity as the proxy does not account for implementation lags. Instead

Mertens and Ravn (2012) propose a proxy based on exogenous tax changes where legislation and implementation are less than a quarter apart. Using this measure, Mertens and Ravn (2014) estimate tax multipliers that lie towards the upper end of the range of estimates.

While a number of studies have attempted to pin down the average estimate of taxation shocks, there is little existing evidence regarding changes in the transmission of this shock across time. An exception is Perotti (2005) who uses sub-sample estimates of the Blanchard and Perotti (2002) SVAR and finds some evidence of a decline in the impact of taxation shocks. In contrast, Mertens and Ravn (2014) show that this sub-sample evidence is much weaker when their proxy VAR is used to estimate the effects of tax shocks.

In this section, we re-visit this question by using our MCMC algorithm to estimate a time-varying proxy SVAR with the tax shock identified with the help of the narrative shock measure of Mertens and Ravn (2012).

4.1 Empirical model, data and priors

We estimate a TVP proxy SVAR(4) model using our MCMC algorithm. The model is

$$Y_t = B_t X_t + u_t$$

where X_t contains four lags and an intercept $X_t = [Y'_{t-1}, \dots, Y'_{t-4}, 1]'$ and $\text{var}(u_t|A_t) = A_t A_t'$. The elements of the coefficient matrices B_t , and A_t evolve over time as random walks, subject to stability condition for B_t . The endogenous variables include (i) real per-capita federal government revenue (T_t), (ii) real per-capita federal government spending (G_t), and (iii) real per-capita GDP (I_t). As described in the technical Appendix, Government spending is defined as the sum of federal government consumption and investment. Taxes are calculated as current receipts of the federal government plus contributions for social insurance less corporate income taxes from Federal

Reserve banks. Both variables are deflated by the GDP deflator and divided by total population. The variables enter the model in log differences and the sample period runs from 1948Q2 to 2016Q2. Note that the tax shock proxy is only available from 1950Q1 to 2006Q4 and the missing observations are estimated as additional states in the model.

The prior for Q^b is set using OLS estimates of the VAR over a training sample of $T_0 = 50$ observations. The priors for Q^a and Q^h have prior degrees of freedom of 15 to give some weight to the prior belief that changes in A_t are gradual. We set loose priors for the instrument equation parameters β and σ^2 in the benchmark case: $p(\beta) \sim \mathcal{N}(0.1, 1)$, $p(\sigma^2) \sim \mathcal{IG}^*(0.05, 1)$. We compare this with an alternative set of priors that incorporates the belief that the instrument is strongly relevant. Under this prior belief: $p(\beta) \sim \mathcal{N}(0.15, 10^{-5})$ while $p(\sigma^2)$ remains $G_2(0.05, 1)$. When setting the prior for q_1 , we incorporate the belief that tax increases should reduce output.¹ As discussed in Mertens and Ravn (2014), compared to views on the size of the impact of tax shocks, this belief on the sign of the impact is relatively uncontroversial.

The MCMC algorithm uses 100,000 replications with a burn-in period of 50,000. Every 10th remaining draw is used for inference. The particle Gibbs step employs 10 particles. The technical appendix presents some evidence for convergence of the algorithm.

4.1.1 Empirical Results

Following Caldara and Herbst (2016), we consider the relevance of the tax shock instrument by calculating the reliability statistic (ρ) of Mertens and Ravn (2013) given in equation 9 above. The estimated posterior distribution of this statistic under the benchmark prior suggests that within our TVP setting, reliability of this instrument is lower than that reported in Mertens and Ravn (2014) for a fixed coefficient model. The median estimate of ρ is 0.08, albeit with the 68 percent

¹This is implemented by rejecting draws from the candidate density in Step 3 of the estimation algorithm that fail to satisfy this belief. Rogers *et al.* (2016) also incorporate inequality restrictions in their application to monetary policy.

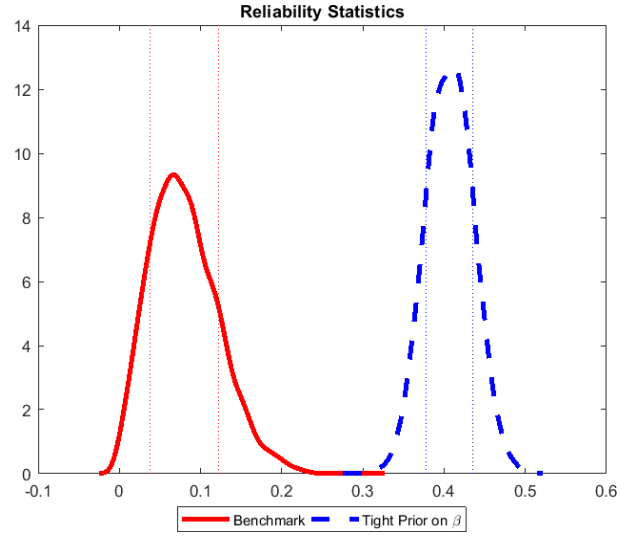


Figure 2: Reliability statistic. The thick line shows the posterior density estimate with the vertical lines displaying the 68 percent error bands.

error band that does not include zero. In contrast, under the prior that essentially fixes $\beta = 0.15$, ρ increases to 0.4. Therefore, in this case, the signal to noise ratio of the instrument is assumed to be high a priori. In the estimates presented below, we consider the importance of this prior belief.

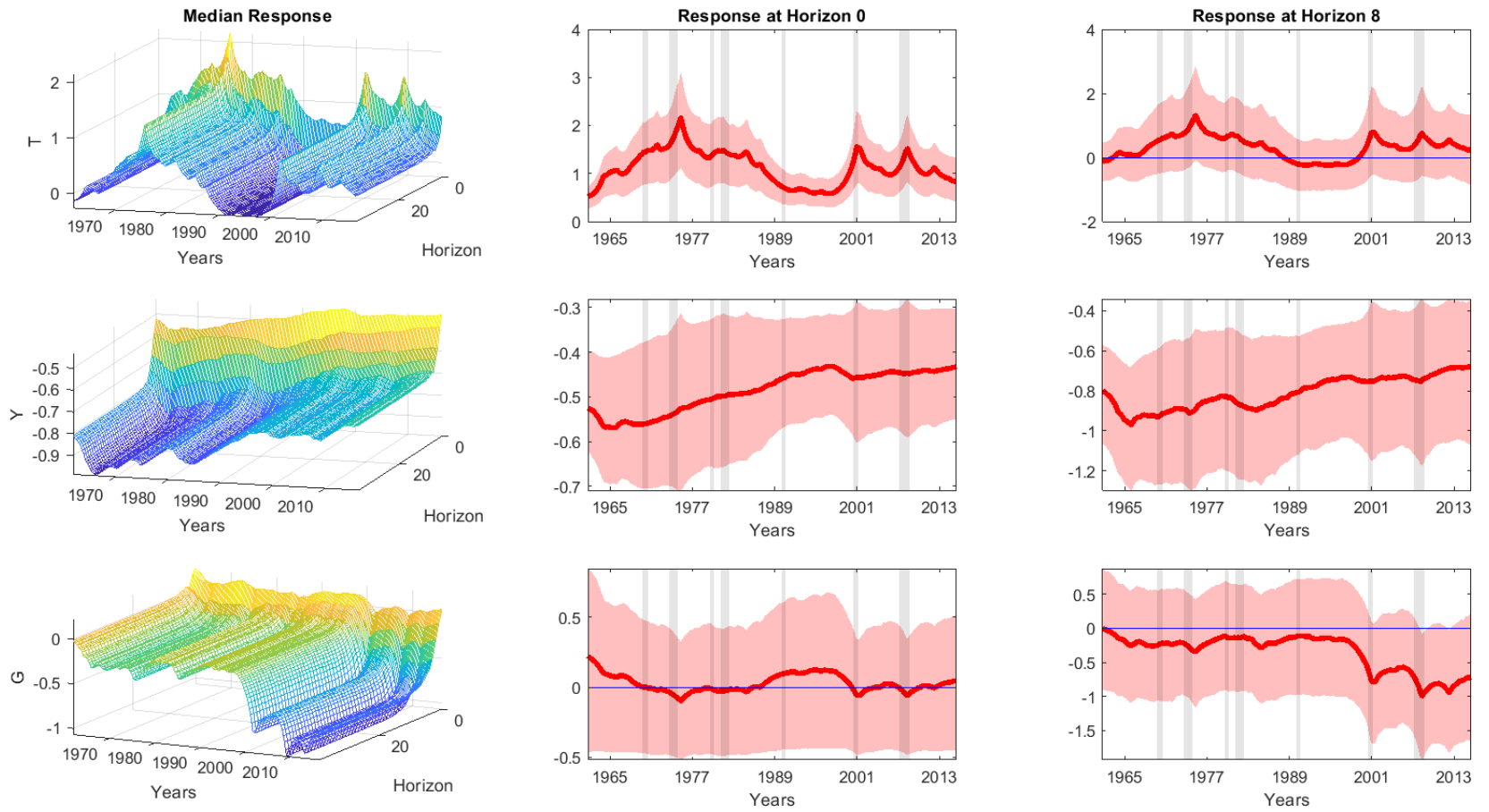


Figure 3: Impulse response to a 1 standard deviation taxation shock

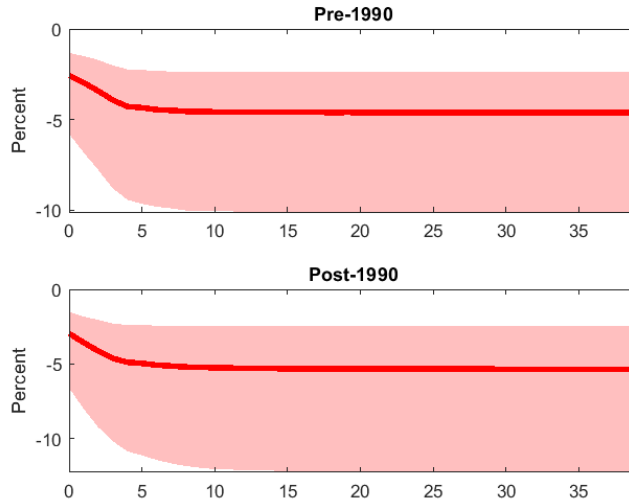


Figure 4: Response of output to a tax increase of one percent of GDP

Figure 3 displays the response of I_t and G_t to a one standard deviation shock to T_t using the benchmark prior for β and σ^2 . The top panel of the Figure shows that the magnitude of the shock is larger before the mid-1980s with the shock volatility increasing again after the early 2000s. This corresponds with an increase in the magnitude of the response of G_t to this shock (final panel of the Figure). The middle panel of the figure shows that the response of output to this shock has declined over time especially at longer horizons. However, this decline mainly appears to reflect the fall in the volatility of the tax shock. Figure 4 shows the average response of I_t to a tax shock before and after 1990, that is scaled to equal one percent of GDP. While the estimation uncertainty is large, the median response is broadly similar to that reported by Mertens and Ravn (2014) for the full sample.

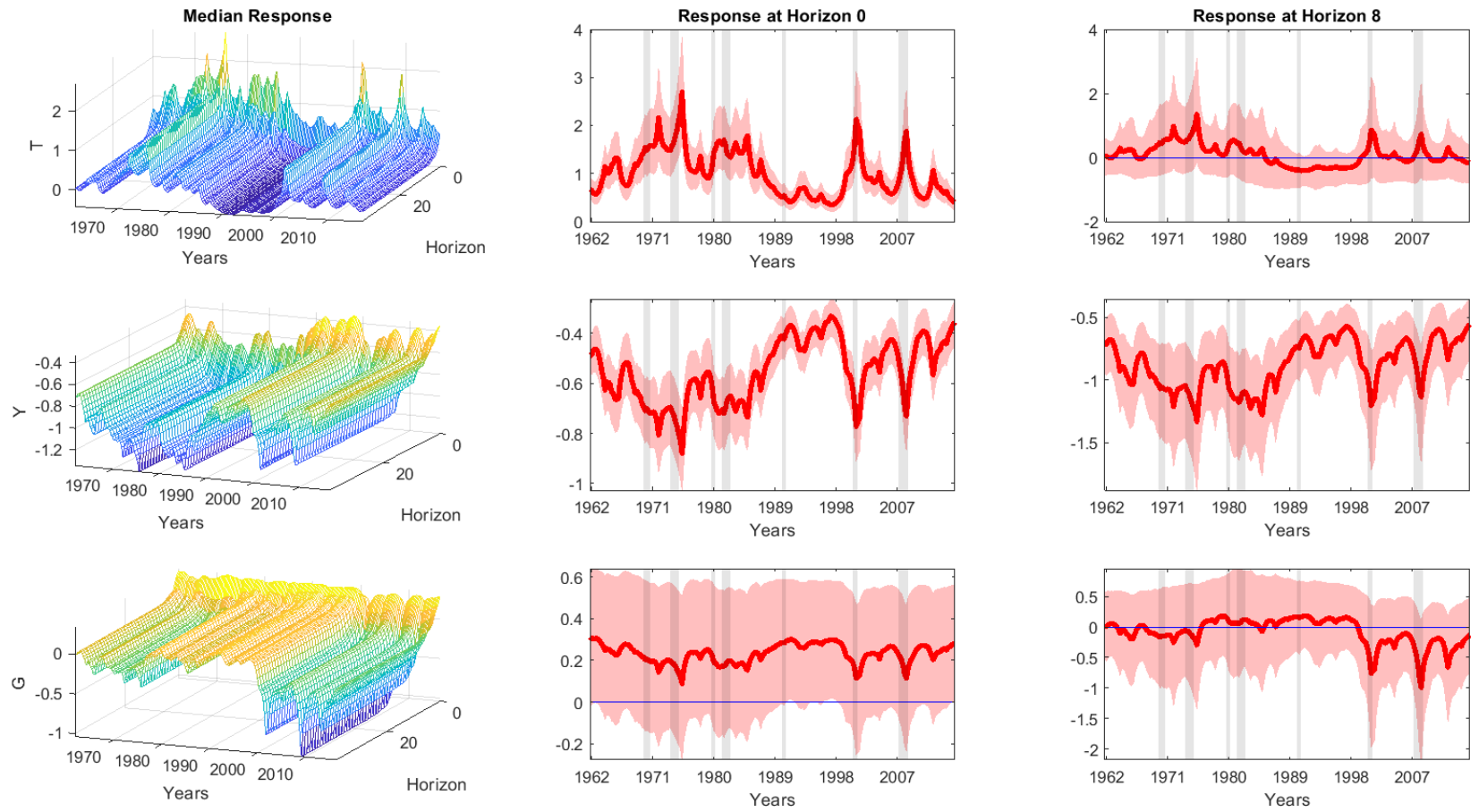


Figure 5: Impulse response to a 1 standard deviation taxation shock. The estimates are based on a tight prior for β

Figure 5 considers the impulse response functions when instrument reliability is assumed to be high a priori. These estimates suggest a number of conclusions. First, the time-variation in the responses is more pronounced at higher frequencies. In other words, the responses change less smoothly than in the benchmark case and display more variation in the short-run. Second, the error bands for the response of output are less wide. This suggests that inference is sharpened by incorporating a higher signal from the tax instrument. Finally, while these responses are more volatile through time, the economic conclusions regarding the transmission of the tax shock are unaltered. Changes in the response of I_t to this shock largely reflect changes in the volatility of the tax shock.

5 Conclusion

This paper proposes a time-varying proxy SVAR model that can be used to estimate changes in the transmission of shocks. We provide a Gibbs sampling algorithm to approximate the posterior distribution of the parameters. Using a simple simulation experiment, we show that the algorithm displays a reasonable performance. The proposed model is used to estimate the time-varying response to tax shocks in the US. Our results suggest that while the volatility of tax shocks has declined, there is limited evidence to suggest a change in the transmission of this shock to output.

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